## Math 120: Quiz 1

Time limit: 20 mins


Let the vector field representing the blizzard be $\vec{F}(x, y)=\langle 1-y \sin (x y),-x \sin (x y)\rangle$.

1. Is $\vec{F}$ conservative? [2 points]
2. Evaluate the line integral $\int_{C_{1}} \vec{F} \cdot d \vec{r}$ where $C_{1}$ is the path from $(-1 / 2,-1 / 2)$ to $(1 / 2,-1 / 2)$ as shown above. [4 points]
3. Evaluate the line integral $\int_{C_{2}} \vec{F} \cdot d \vec{r}$ where $C_{2}$ is the circle of radius 1 centered at the origin oriented counter-clockwise. [1 point]
4. Suppose a gust of wind changes the vector field $\vec{F}$ to a new vector field $\vec{G}=\vec{F}+\langle y, 0\rangle$. Evaluate the line integral

$$
\int_{C_{2}} \vec{G} \cdot d \vec{r}
$$

where $C_{2}$ is the same circle as above. [3 points]

